

## Atomic Theory 1.7

### Quantum Numbers

### The Four Quantum Numbers

$n \rightarrow$  Principal Quantum Number

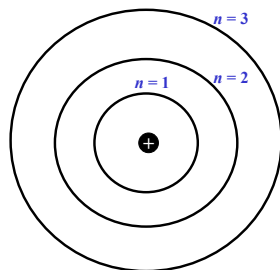
$l \rightarrow$  Angular Momentum Quantum Number

$m \rightarrow$  Magnetic Quantum Number

$m_s \rightarrow$  Electronic Spin Quantum Number

### Principal Quantum Number ( $n$ )

$n = 1, 2, 3, 4, 5, 6, 7$



All electrons that have the same ' $n$ ' value are described as being in the same '**shell**'.

### Angular Momentum Quantum Number ( $l$ )

$$l = 0, 1, 2, \dots, (n - 1)$$

Any principal quantum number ( $n$ ), may contain sublevels from 0 to  $n - 1$ .

$n = 1$  has one sublevel ( $l = 0$ )

$n = 2$  may have two sublevels ( $l = 0$  and  $l = 1$ )

$n = 3$  may have three sublevels ( $l = 0, 1,$  and  $2$ )

### Angular Momentum Quantum Number ( $l$ )

( $l$ ) Defines the shape or type of orbital

$l$	0	1	2	3
Type of Orbital	s	p	d	f

### Magnetic Quantum Number ( $m$ )

$$m = -l \text{ to } +l$$

$m \rightarrow$  Defines the orientation of the orbital in three dimensional space.

### Quantum Numbers when $n = 1$

When  $n = 1$

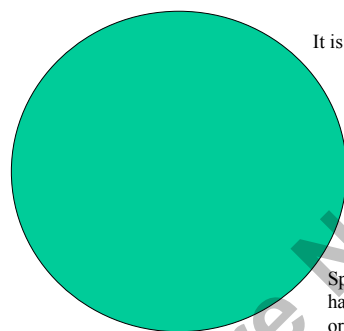
$$l = 0$$

$n = 1$  can only have a s-orbital

$$m = 0$$

which means there is only one orientation

### 1s Orbital



It is spherical.

Spheres can only have one orientation.

### Quantum Numbers when $n = 2$

When  $n = 2$

$$l = 0$$

Which defines a **s-orbital**

and

$$l = 1$$

Which defines a **p-orbital**

So  $n = 2$  can have s and p-orbitals.

### Quantum Numbers when $n = 2$

Again, when  $l = 0, m = 0$ .

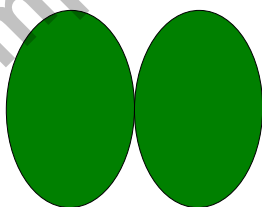
There is one orientation, as it is an s-orbital.

When  $l = 1, m$  can be  $-1, 0, \text{ or } +1$ .

There are three orientations for a p-orbital.

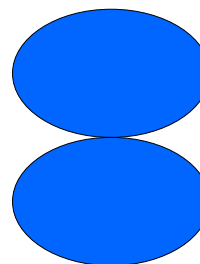
**$p_x, p_y, \text{ and } p_z$**

There are three 2p orbitals



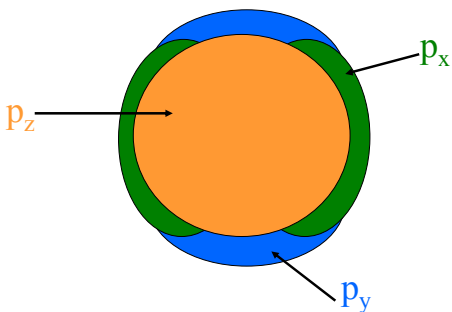
$p_x$

There are three 2p orbitals



$p_y$

### The three p-orbitals together



### Quantum Numbers when $n = 3$

When  $n = 3$

$l = 0$  (s-orbital)

$l = 1$  (p-orbital)

or  $l = 2$  (d-orbital)

$m = -2, -1, 0, +1, \text{ or } +2$

Thus, there are 5 d-orbitals.

### Quantum Numbers when $n = 4$

When  $n = 4$

$l = 0$  (s-orbital)

$l = 1$  (p-orbital)

$l = 2$  (d-orbital)

$l = 3$  (f-orbital)

$m = -3, -2, -1, 0, +1, +2, \text{ or } +3$

Thus, there are 7 f-orbitals.

### Electron Spin Quantum Number ( $m_s$ )

$$m_s = +\frac{1}{2} \text{ or } -\frac{1}{2}$$

- There is a maximum of two electrons per orbital.
- They spin in opposite directions.
- Spin up or spin down

### Pauli's Exclusion Principle

It is not possible for two electrons in an atom to have the same four quantum numbers.

### Ex) Quantum Numbers

Ex) What are the possible angular momentum, magnetic, and electron spin quantum numbers associated with a single electron in a p-orbital of  $n = 3$ ?